ANALOG DEVICES

Low Noise, Matched Dual Monolithic Transistor
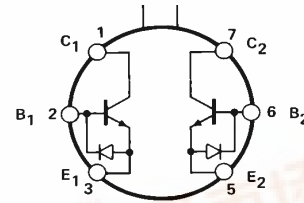
MAT02

FEATURES
Low Offset Voltage: 50 µV max
Low Noise Voltage at 100 Hz, 1 mA: 1.0 nV/$\sqrt{Hz}$ max
High Gain (h_{FE}): 500 min at I_C = 1 mA
               300 min at I_C = 1 µA
Excellent Log Conformance: $r_{BE} \simeq 0.3\ \Omega$
Low Offset Voltage Drift: 0.1 µV/°C max
Improved Direct Replacement for LM194/394
Available in Die Form

PIN CONNECTION
TO-78
(H Suffix)

NOTE
Substrate is connected to case on TO-78 package. Substrate is normally connected to the most negative circuit potential, but can be floated.

PRODUCT DESCRIPTION
The design of the MAT02 series of NPN dual monolithic transistors is optimized for very low noise, low drift, and low r_{BE}. Precision Monolithics' exclusive Silicon Nitride "Triple-Passivation" process stabilizes the critical device parameters over wide ranges of temperature and elapsed time. Also, the high current gain (h_{FE}) of the MAT02 is maintained over a wide range of collector current. Exceptional characteristics of the MAT02 include offset voltage of 50 µV max (A/E grades) and 150 µV max F grade. Device performance is specified over the full military temperature range as well as at 25°C.

Input protection diodes are provided across the emitter-base junctions to prevent degradation of the device characteristics due to reverse-biased emitter current. The substrate is clamped to the most negative emitter by the parasitic isolation junction created by the protection diodes. This results in complete isolation between the transistors.

The MAT02 should be used in any application where low noise is a priority. The MAT02 can be used as an input stage to make an amplifier with noise voltage of less than 1.0 nV/$\sqrt{Hz}$ at 100 Hz. Other applications, such as log/antilog circuits, may use the excellent logging conformity of the MAT02. Typical bulk resistance is only 0.3 Ω to 0.4 Ω. The MAT02 electrical characteristics approach those of an ideal transistor when operated over a collector current range of 1 µA to 10 mA. For applications requiring multiple devices see MAT04 Quad Matched Transistor data sheet.

ABSOLUTE MAXIMUM RATINGS[1]
Collector-Base Voltage (BV_{CBO}) . . . . 40 V
Collector-Emitter Voltage (BV_{CEO}) . . . . 40 V
Collector-Collector Voltage (BV_{CC}) . . . . 40 V
Emitter-Emitter Voltage (BV_{EE}) . . . . 40 V
Collector Current (I_C) . . . . 20 mA
Emitter Current (I_E) . . . . 20 mA
Total Power Dissipation
   Case Temperature ≤ 40°C[2] . . . . 1.8 W
   Ambient Temperature ≤ 70°C[3] . . . . 500 mW
Operating Temperature Range
   MAT02A . . . . −55°C to +125°C
   MAT02E, F . . . . −25°C to +85°C
Operating Junction Temperature . . . . −55°C to +150°C
Storage Temperature . . . . −65°C to +150°C
Lead Temperature (Soldering, 60 sec) . . . . +300°C
Junction Temperature . . . . −65°C to +150°C

NOTES
[1]Absolute maximum ratings apply to both DICE and packaged devices.
[2]Rating applies to applications using heat sinking to control case temperature. Derate linearly at 16.4 mW/°C for case temperature above 40°C.
[3]Rating applies to applications not using a heat sinking; devices in free air only. Derate linearly at 6.3 mW/°C for ambient temperature above 70°C.

ORDERING GUIDE[1]

Model	V_{OS} max (T_A = +25°C)	Temperature Range	Package Option
MAT02AH[2]	50 µV	−55°C to +125°C	TO-78
MAT02EH	50 µV	−55°C to +125°C	TO-78
MAT02FH	150 µV	−55°C to +125°C	TO-78

NOTES
[1]Burn-in is available on commercial and industrial temperature range parts in TO-can packages.
[2]For devices processed in total compliance to MIL-STD-883, add /883 after part number. Consult factory for 883 data sheet.

REV. C

MAT02–SPECIFICATIONS

ELECTRICAL CHARACTERISTICS (@ V_{CB} = 15 V, I_C = 10 μA, T_A = 25°C, unless otherwise noted.)

Parameter	Symbol	Conditions	MAT02A/E			MAT02F			Units
			Min	Typ	Max	Min	Typ	Max	
Current Gain	h_{FE}	I_C = 1 mA[1]	500	605		400	605		
		I_C = 100 μA	500	590		400	590		
		I_C = 10 μA	400	550		300	550		
		I_C = 1 μA	300	485		200	485		
Current Gain Match	Δh_{FE}	10 μA ≤ I_C ≤ 1 mA[2]		0.5	2		0.5	4	%
Offset Voltage	V_{OS}	V_{CB} = 0, 1 μA ≤ I_C ≤ 1 mA[3]		10	50		80	150	μV
Offset Voltage	$\Delta V_{OS}/\Delta V_{CB}$	0 ≤ V_{CB} ≤ V_{MAX},[4]		10	25		10	50	μV
Change vs. V_{CB}		1 μA ≤ I_C ≤ 1 mA[3]		10	25		10	50	μV
Offset Voltage Change	$\Delta V_{OS}/\Delta I_C$	V_{CB} = 0 V		5	25		5	50	μV
vs. Collector Current		1 μA ≤ I_C ≤ 1 mA[3]		5	25		5	50	μV
Offset Current									
Change vs. V_{CB}	$\Delta I_{OS}/\Delta V_{CB}$	0 ≤ V_{CB} ≤ V_{MAX}		30	70		30	70	pA/V
Bulk Resistance	r_{BE}	10 μA ≤ I_C ≤ 10 mA[5]		0.3	0.5		0.3	0.5	Ω
Collector-Base									
Leakage Current	I_{CBO}	V_{CB} = V_{MAX}		25	200		25	400	pA
Collector-Collector									
Leakage Current	I_{CC}	V_{CC} = V_{MAX}[5, 6]		35	200		35	400	pA
Collector-Emitter		V_{CE} = V_{MAX}[5, 6]							
Leakage Current	I_{CES}	V_{BE} = 0		35	200		35	400	pA
Noise Voltage Density	e_n	I_C = 1 mA, V_{CB} = 0[7]							
		f_O = 10 Hz		1.6	2		1.6	3	nV/$\sqrt{\text{Hz}}$
		f_O = 100 Hz		0.9	1		0.9	2	nV/$\sqrt{\text{Hz}}$
		f_O = 1 kHz		0.85	1		0.85	2	nV/$\sqrt{\text{Hz}}$
		f_O = 10 kHz		0.85	1		0.85	2	nV/$\sqrt{\text{Hz}}$
Collector Saturation									
Voltage	$V_{CE(SAT)}$	I_C = 1 mA, I_B = 100 μA		0.05	0.1		0.05	0.2	V
Input Bias Current	I_B	I_C = 10 μA			25			34	nA
Input Offset Current	I_{OS}	I_C = 10 μA			0.6			1.3	nA
Breakdown Voltage	BV_{CEO}		40			40			V
Gain-Bandwidth Product	f_T	I_C = 10 mA, V_{CE} = 10 V		200			200		MHz
Output Capacitance	C_{OB}	V_{CB} = 15 V, I_E = 0		23			23		pF
Collector-Collector									
Capacitance	C_{CC}	V_{CC} = 0		35			35		pF

NOTES

[1] Current gain is guaranteed with Collector-Base Voltage (V_{CB}) swept from 0 to V_{MAX} at the indicated collector currents.

[2] Current gain match (Δh_{FE}) is defined as: $\Delta h_{FE} = \dfrac{100\,(\Delta I_B)\,(h_{FE}\,\text{min})}{I_C}$

[3] Measured at I_C = 10 μA and guaranteed by design over the specified range of I_C.

[4] This is the maximum change in V_{OS} as V_{CB} is swept from 0 V to 40 V.

[5] Guaranteed by design.

[6] I_{CC} and I_{CES} are verified by measurement of I_{CBO}.

[7] Sample tested.

Specifications subject to change without notice.

ELECTRICAL CHARACTERISTICS (V_{CB} = 15 V, −25°C ≤ T_A ≤ +85°C, unless otherwise noted.)

Parameter	Symbol	Conditions	MAT02E Min	Typ	Max	MAT02F Min	Typ	Max	Units
Offset Voltage	V_{OS}	V_{CB} = 0 1 μA ≤ I_C ≤ 1 mA[1]			70			220	μV
Average Offset Voltage Drift	TCV_{OS}	10 μA ≤ I_C ≤ 1 mA, 0 ≤ V_{CB} ≤ V_{MAX}[2] V_{OS} Trimmed to Zero[3]		0.08 0.03	0.3 0.1		0.08 0.03	1 0.3	μV/°C
Input Offset Current	I_{OS}	I_C = 10 μA			8			13	nA
Input Offset Current Drift	TCI_{OS}	I_C = 10 μA[4]		40	90		40	150	pA/°C
Input Bias Current	I_B	I_C = 10 μA			45			50	nA
Current Gain	h_{FE}	I_C = 1 mA[5] I_C = 100 μA I_C = 10 μA I_C = 1 μA	325 275 225 200			300 250 200 150			
Collector-Base Leakage Current	I_{CBO}	V_{CB} = V_{MAX}		2			3		nA
Collector-Emitter Leakage Current	I_{CES}	V_{CE} = V_{MAX}, V_{BE} = 0		3			4		nA
Collector-Collector Leakage Current	I_{CC}	V_{CC} = V_{MAX}		3			4		nA

ELECTRICAL CHARACTERISTICS (V_{CB} = 15 V, −55°C ≤ T_A ≤ +125°C, unless otherwise noted.)

Parameter	Symbol	Conditions	MAT02A Min	Typ	Max	Units
Offset Voltage	V_{OS}	V_{CB} = 0 1 μA ≤ I_C ≤ 1 mA[1]			80	μV
Average Offset Voltage Drift	TCV_{OS}	10 μA ≤ I_C ≤ 1 mA, 0 ≤ V_{CB} ≤ V_{MAX}[2] V_{OS} Trimmed to Zero[3]		0.08 0.03	0.3 0.1	μV/°C μV/°C
Input Offset Current	I_{OS}	I_C = 10 μA			9	nA
Input Offset Current Drift	TCI_{OS}	I_C = 10 μA[4]		40	90	pA/°C
Input Bias Current	I_B	I_C = 10 μA			60	nA
Current Gain	h_{FE}	I_C = 1 mA[5] I_C = 100 μA I_C = 10 μA I_C = 1 μA	275 225 125 150			
Collector-Base Leakage Current	I_{CBO}	V_{CB} = V_{MAX} T_A = 125°C			15	nA
Collector-Emitter Leakage Current	I_{CES}	V_{CE} = V_{MAX}, V_{BE} = 0 T_A = 125°C			50	nA
Collector-Collector Leakage Current	I_{CC}	V_{CC} = V_{MAX} T_A = 125°C			30	nA

NOTES
[1]Measured at I_C = 10 μA and guaranteed by design over the specified range of I_C.

[2]Guaranteed by V_{OS} test $(TCV_{OS} \cong \frac{V_{OS}}{T}$ for $V_{OS} \ll V_{BE})$ $T = 298°K$ for T_A = 25°C.

[3]The initial zero offset voltage is established by adjusting the ratio of IC1 to IC2 at T_A = 25°C. This ratio must be held to 0.003% over the entire temperature range. Measurements are taken at the temperature extremes and 25 °C.

[4]Guaranteed by design.

[5]Current gain is guaranteed with Collector-Base Voltage (V_{CB}) swept from 0 to V_{MAX} at the indicated collector current.

Specifications subject to change without notice.

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WAFER TEST LIMITS (@ 25°C for V_{CB} = 15 V and I_C = 10 μA, unless otherwise noted.)

Parameter	Symbol	Conditions	MAT02N Limits	Units
Breakdown Voltage	BV_{CEO}		40	V min
Offset Voltage	V_{OS}	10 μA ≤ I_C ≤ 1 mA[1]	150	μV max
Input Offset Current	I_{OS}		1.2	nA max
Input Bias Current	I_B	V_{CB} = 0 V	34	nA max
Current Gain	h_{FE}	I_C = 1 mA, V_{CB} = 0 V	400	min
		I_C = 10 μA, V_{CB} = 0 V	300	
Current Gain Match	Δh_{FE}	10 μA ≤ I_C ≤ 1 mA, V_{CB} = 0 V	4	% max
Offset Voltage Change vs. V_{CB}	$\Delta V_{OS}/\Delta V_{CB}$	0 V ≤ V_{CB} ≤ 40 V 10 μA ≤ I_C ≤ 1 mA[1]	50	μV max
Offset Voltage Change vs. Collector Current	$\Delta V_{OS}/\Delta I_C$	V_{CB} = 0 10 μA ≤ I_C ≤ 1 mA[1]	50	μV max
Bulk Resistance	r_{BE}	100 μA ≤ I_C ≤ 10 mA	0.5	Ω max
Collector Saturation Voltage	$V_{CE\,(SAT)}$	I_C = 1 mA I_B = 100 μA	0.2	V max

NOTES
[1]Measured at I_C = 10 μA and guaranteed by design over the specified range of I_C.

Electrical tests are performed at wafer probe to the limits shown. Due to variations in assembly methods and normal yield loss, yield after packaging is not guaranteed for standard product dice. Consult factory to negotiate specifications based on dice lot qualification through sample lot assembly and testing.

TYPICAL ELECTRICAL CHARACTERISTICS (V_{CB} = 15 V, I_C = 10 μA, T_A = +25°C, unless otherwise noted.)

Parameter	Symbol	Conditions	MAT02N Limits	Units
Average Offset Voltage Drift	TCV_{OS}	10 μA ≤ I_C ≤ 1 mA 0 ≤ V_{CB} ≤ V_{MAX}	0.08	μV/°C
Average Offset Current Drift	TCI_{OS}	I_C = 10 μA	40	pA/°C
Gain-Bandwidth Product	f_T	V_{CE} = 10 V, I_C = 10 mA	200	MHz
Offset Current Change vs. V_{CB}	$\Delta I_{OS}/\Delta V_{CB}$	0 ≤ V_{CB} ≤ 40 V	70	pA/V

DICE CHARACTERISTICS
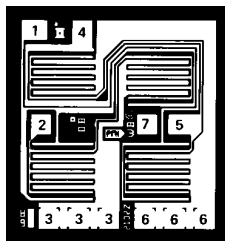
1. COLLECTOR (1)
2. BASE (1)
3. EMITTER (1)
4. COLLECTOR (2)
5. BASE (2)
6. EMITTER (2)
7. SUBSTRATE

Die Size 0.061 × 0.057 inch, 3,477 sq. mils
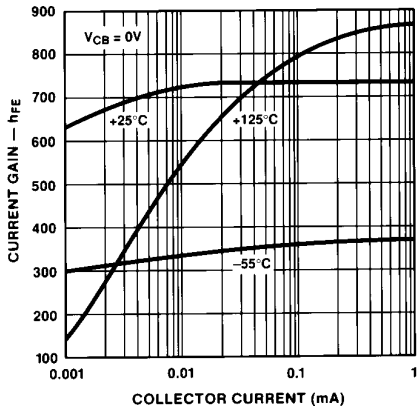*(1.549 × 1.448 mm, 224 sq. mm)*

Figure 1. Current Gain vs.
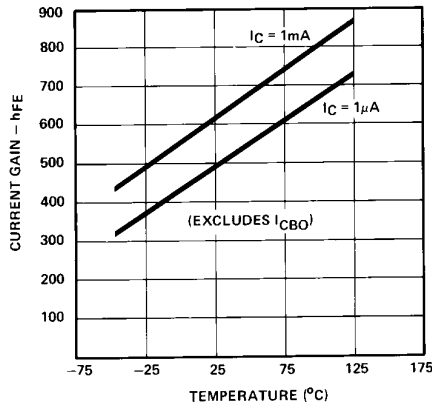Collector Current

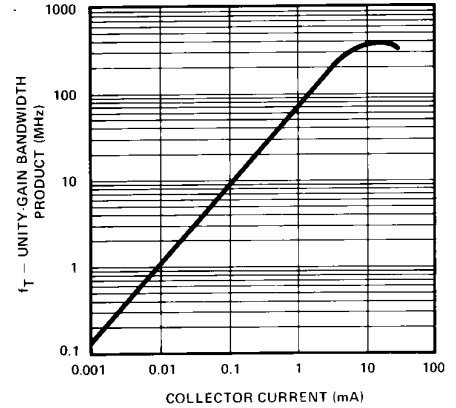Figure 2. Current Gain
vs. Temperature
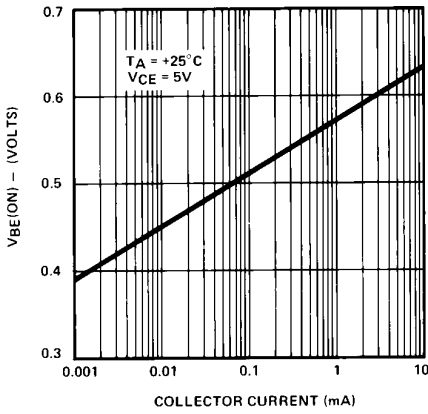
Figure 3. Gain Bandwidth
vs. Collector Current

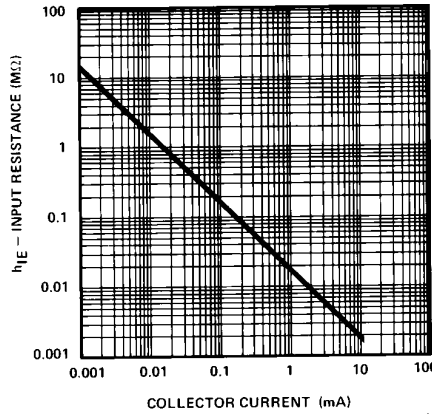Figure 4. Base-Emitter-On
Voltage vs. Collector Current

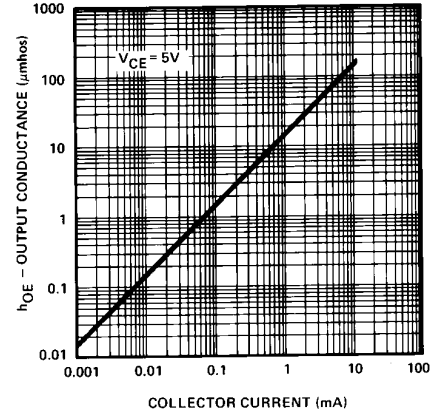Figure 5. Small Signal Input
Resistance vs. Collector Current

Figure 6. Small-Signal Output
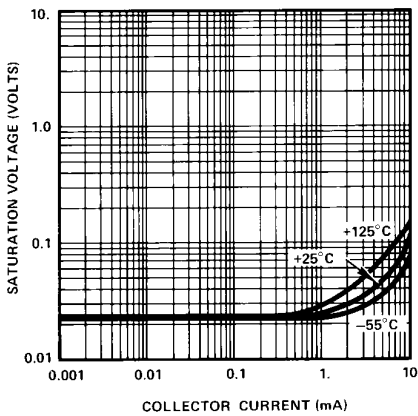Conductance vs. Collector Current
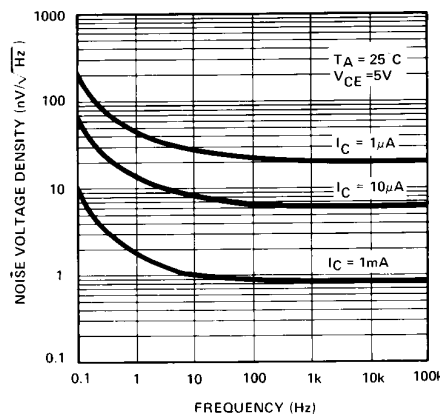
Figure 7. Saturation Voltage
vs. Collector Current

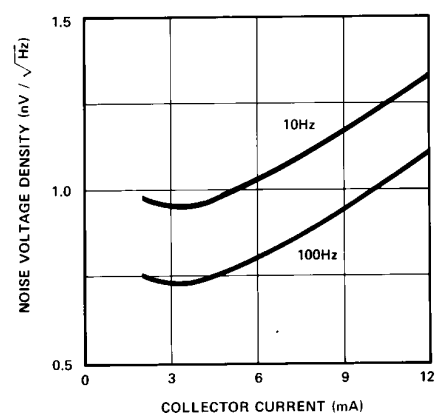Figure 8. Noise Voltage
Density vs. Frequency

Figure 9. Noise Voltage Density
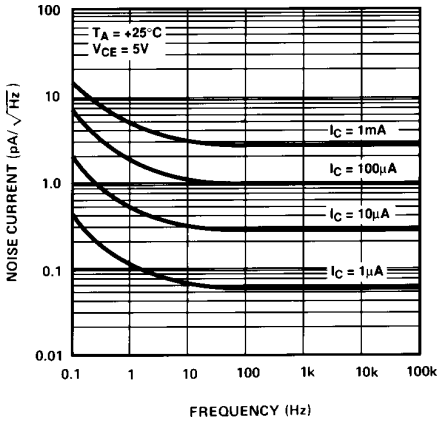vs. Collector Current

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Figure 10. Noise Current
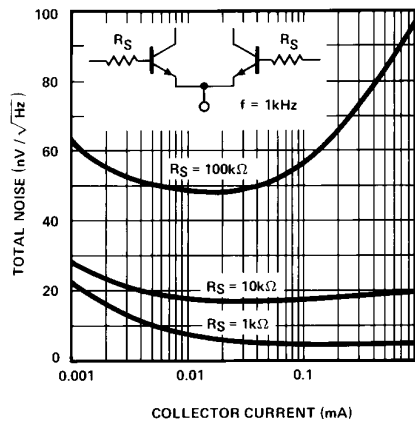Density vs. Frequency

Figure 11. Total Noise vs.
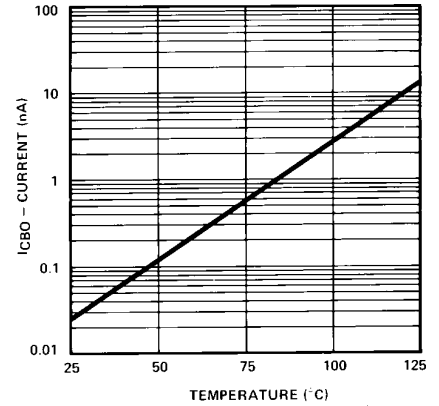Collective Current

Figure 12. Collector-to-Base
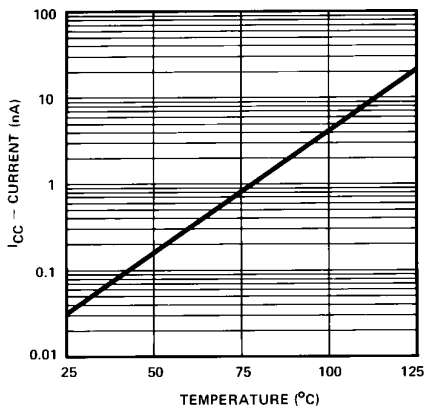Leakage vs. Temperature

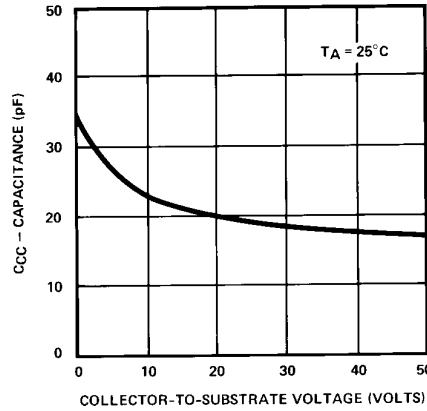Figure 13. Collector-to-Collector
Leakage vs. Temperature

Figure 14. Collector-to-Collector
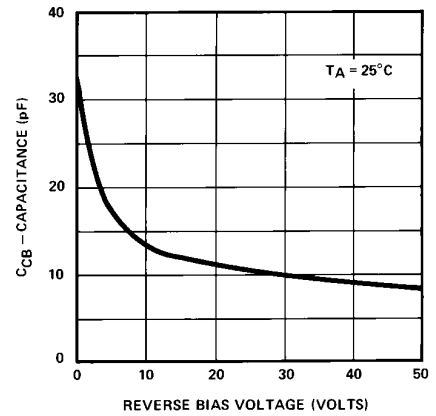Capacitance vs. Collector-to
Substrate Voltage

Figure 15. Collector-Base
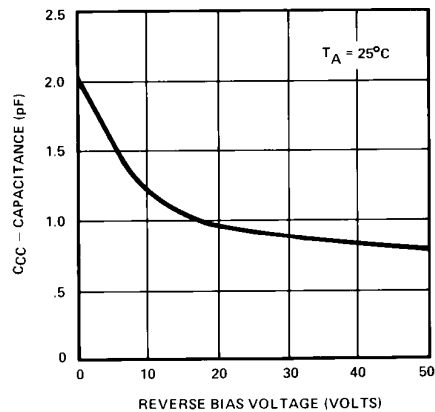Capacitance vs. Reverse Bias Voltage

Figure 16. Collector-to-Collector
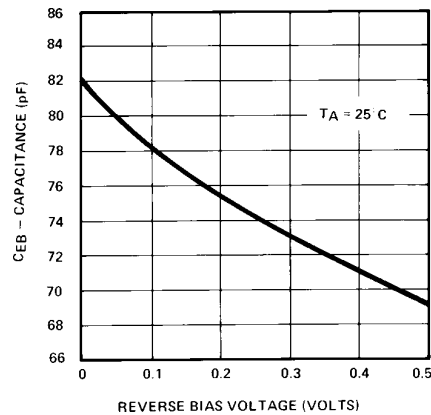Capacitance vs. Reverse Bias Voltage

Figure 17. Emitter-Base Capacitance
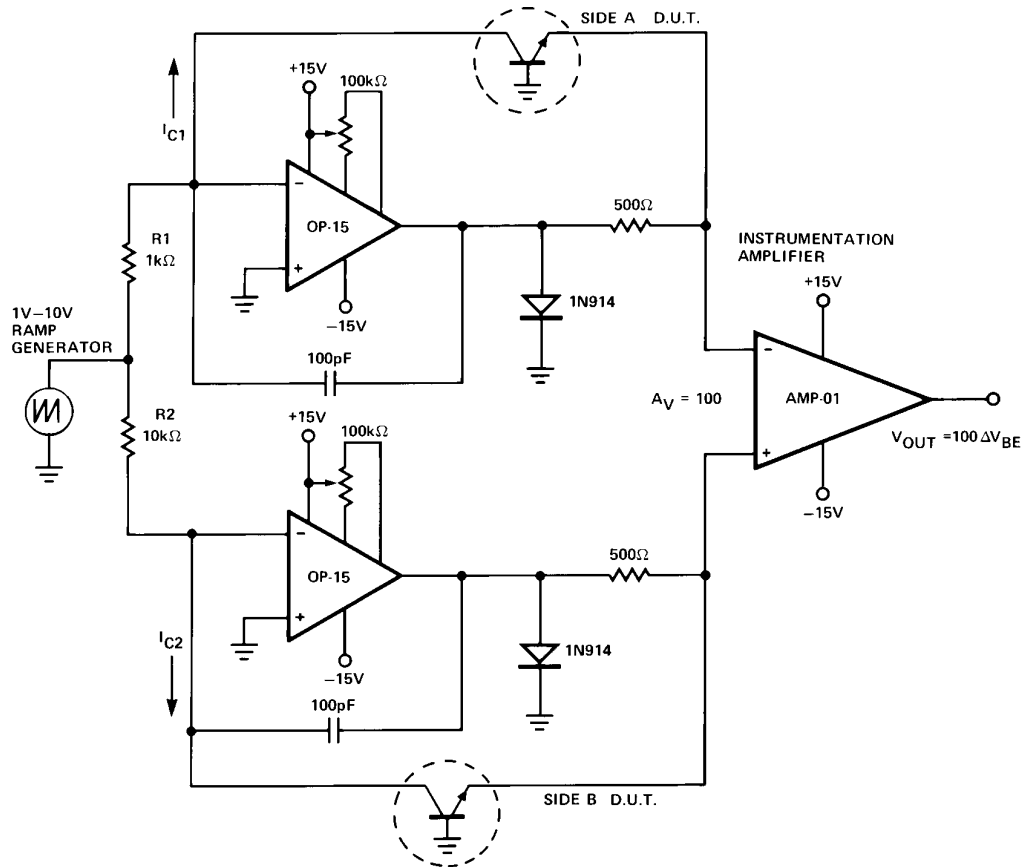vs. Reverse Bias Voltage

Figure 18. Log Conformance Test Circuit

LOG CONFORMANCE TESTING

The log conformance of the MAT02 is tested using the circuit shown above. The circuit employs a dual transdiode logarithmic converter operating at a fixed ratio of collector currents that are swept over a 10:1 range. The output of each transdiode converter is the V_{BE} of the transistor plus an error term which is the product of the collector current and r_{BE}, the bulk emitter resistance. The difference of the V_{BE} is amplified at a gain of ×100 by the AMP01 instrumentation amplifier. The differential emitter-base voltage (ΔV_{BE}) consists of a temperature-dependent dc level plus an ac error voltage which is the deviation from true log conformity as the collector currents vary.

The output of the transdiode logarithmic converter comes from the idealized intrinsic transistor equation (for silicon):

$$V_{BE} = \frac{kT}{q} In\frac{I_C}{I_S} \text{ where} \tag{1}$$

k = Boltzmann's Constant (1.38062×10^{-23} J/°K)

q = Unit Electron Charge (1.60219×10^{-19} °C)

T = Absolute Temperature, °K (= °C + 273.2)

I_S = Extrapolated Current for $V_{BE} \rightarrow 0$

I_C = Collector Current

An error term must be added to this equation to allow for the bulk resistance (r_{BE}) of the transistor. Error due to the op amp input current is limited by use of the OP15 BiFET-input op amp. The resulting AMP01 input is:

$$\Delta V_{BE} = \frac{kT}{q} In\frac{I_{C1}}{I_{C2}} + I_{C1}\, r_{BE1} - I_{C2}\, r_{BE2} \tag{2}$$

A ramp function which sweeps from 1 V to 10 V is converted by the op amps to a collector current ramp through each transistor. Because I_{C1} is made equal to 10 I_{C2}, and assuming $T_A = 25°C$, the previous equation becomes:

$$\Delta V_{BE} = 59\ mV + 0.9\ I_{C1}\, r_{BE}\ (\Delta r_{BE} \sim 0)$$

As viewed on an oscilloscope, the change in ΔV_{BE} for a 10:1 change in I_C is then displayed as shown below:
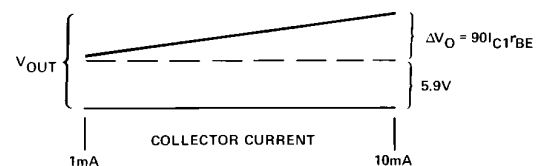
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With the oscilloscope ac coupled, the temperature dependent term becomes a dc offset and the trace represents the deviation from true log conformity. The bulk resistance can be calculated from the voltage deviation ΔV_O and the change in collector current (9 mA):

$$r_{BE} = \frac{\Delta V_O}{9\,mA} \times \frac{1}{100} \tag{3}$$

This procedure finds r_{BE} for Side A. Switching R_1 and R_2 will provide the r_{BE} for Side B. Differential r_{BE} is found by making $R_1 = R_2$.

APPLICATIONS: NONLINEAR FUNCTIONS
MULTIPLIER/DIVIDER CIRCUIT
The excellent log conformity of the MAT02 over a very wide range of collector current makes it ideal for use in log-antilog circuits. Such nonlinear functions as multiplying, dividing, squaring, and square-rooting are accurately and easily implemented with a log-antilog circuit using two MAT02 pairs (see Figure 19). The transistor circuit accepts three input currents (I_1, I_2, and I_3) and provides an output current I_O according to $I_O = I_1 I_2 / I_3$. All four currents must be positive in the log-antilog circuit, but negative input voltages can be easily accommodated

by various offsetting techniques. Protective diodes across each base-to-emitter junction would normally be needed, but these diodes are built into the MAT02. External protection diodes are therefore not needed.

For the circuit shown in Figure 19, the operational amplifiers make $I_1 = V_X/R_1$, $I_2 = V_Y/R_2$, $I_3 = V_Z/R_3$, and $I_O = V_O/R_O$. The output voltage for this one-quadrant, log-antilog multiplier/divider is ideally:

$$V_O = \frac{R_3 R_O}{R_1 R_2} \frac{V_X V_Y}{V_Z} \quad (V_X,\ V_Y,\ V_Z > 0) \tag{4}$$

If all the resistors (R_O, R_1, R_2, R_3) are made equal, then $V_O = V_X V_Y / V_Z$. Resistor values of 50 kΩ to 100 kΩ are recommended assuming an input range of 0.1 V to +10 V.

ERROR ANALYSIS
The base-to-emitter voltage of the MAT02 in its forward active operation is:

$$V_{BE} = \frac{kT}{q} In \frac{I_C}{I_S} + r_{BE} I_C,\ V_{CB} \sim 0 \tag{5}$$

The first term comes from the idealized intrinsic transistor equation previously discussed (see equation (1)).
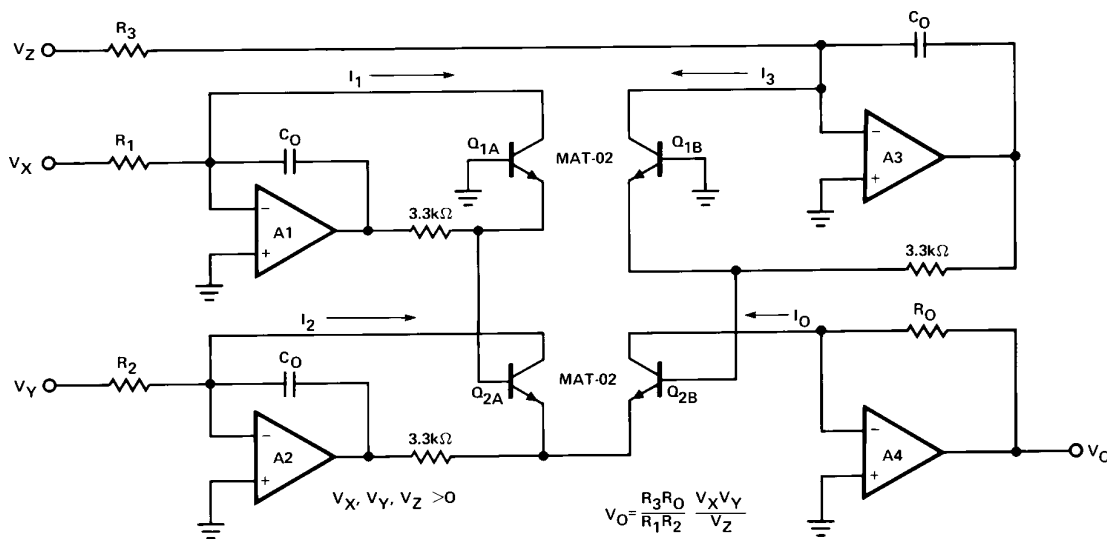

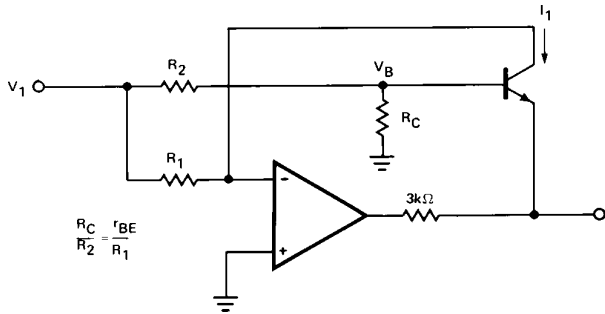Figure 19. One-Quadrant Multiplier/Divider

Figure 20. Compensation of Bulk Resistance Error

Extrinsic resistive terms and the early effect cause departure from the ideal logarithmic relationship. For small V_{CB}, all of these effects can be lumped together as a total effective bulk resistance r_{BE}. The $r_{BE}I_C$ term causes departure from the desired logarithmic relationship. The r_{BE} term for the MAT02 is less than 0.5 Ω and Δr_{BE} between the two sides is negligible.

Returning to the multiplier/divider circuit of Figure 1 and using Equation (4):

$$V_{BE1A} + V_{BE2A} - V_{BE2B} - V_{BE1B} + (I_1 + I_2 - I_O - I_3)\,r_{BE} = 0$$

If the transistor pairs are held to the same temperature, then:

$$\frac{kT}{q} \ln \frac{I_1 I_2}{I_3 I_O} = \frac{kT}{q} \ln \frac{I_{S1A} I_{S2A}}{I_{S1B} I_{S2B}} + (I_1 + I_2 - I_O - I_3)\, r_{BE} \quad (6)$$

If all the terms on the right-hand side were zero, then we would have ln $(I_1\, I_2/I_3\, I_O)$ equal to zero which would lead directly to the desired result:

$$I_O = \frac{I_1 I_2}{I_3}, \text{ where } I_1, I_2, I_3, I_O > 0 \quad (7)$$

Note that this relationship is temperature independent. The right-hand side of Equation (6) is near zero and the output current I_O will be approximately $I_1\, I_2/I_3$. To estimate error, define ø as the right-hand side terms of Equation (6):

$$\text{ø} = \ln \frac{I_{S1A} I_{S2A}}{I_{S1B} I_{S2B}} + \frac{q}{kT}\,(I_1 + I_2 - I_O - I_3)\, r_{BE} \quad (8)$$

For the MAT02, ln (I_{SA}/I_{SB}) and $I_C r_{BE}$ are very small. For small ø, $\varepsilon^{\text{ø}} \sim 1 + \text{ø}$ and therefore:

$$\frac{I_1 I_2}{I_3 I_O} = 1 + \text{ø}$$

$$\quad (9)$$

$$I_O \sim \frac{I_1 I_2}{I_3}\,(1 - \text{ø})$$

The ln (I_{SA}/I_{SB}) terms in ø cause a fixed gain error of less than ±0.6% from each pair when using the MAT02, and this gain error is easily trimmed out by varying R_O. The $I_C r_{BE}$ terms are more troublesome because they vary with signal levels and are multiplied by absolute temperature. At 25°C, kT/q is

approximately 26 mV and the error due to an $r_{BE}I_C$ term will be $r_{BE}I_C/26$ mV. Using an r_{BE} of 0.4 Ω for the MAT02 and assuming a collector current range of up to 200 μA, then a peak error of 0.3% could be expected for an $r_{BE}I_C$ error term when using the MAT02. Total error is dependent on the specific application configuration (multiply, divide, square, etc.) and the required dynamic range. An obvious way to reduce $I_C r_{BE}$ error is to reduce the maximum collector current, but then op amp offsets and leakage currents become a limiting factor at low input levels. A design range of no greater than 10 μA to 1 mA is generally recommended for most nonlinear function circuits.

A powerful technique for reducing error due to $I_C r_{BE}$ is shown in Figure 20. A small voltage equal to $I_C r_{BE}$ is applied to the transistor base. For this circuit:

$$V_B = \frac{R_C}{R_2}\,V_1 \text{ and } I_C r_{BE} = \frac{r_{BE}}{R_1}\,V_1 \quad (10)$$

The error from $r_{BE}I_C$ is cancelled if R_C/R_2 is made equal to r_{BE}/R_1. Since the MAT02 bulk resistance is approximately 0.39 Ω, an R_C of 3.9 Ω and R_2 of 10 R_1 will give good error cancellation.

In more complex circuits, such as the circuit in Figure 19, it may be inconvenient to apply a compensation voltage to each individual base. A better approach is to sum all compensation to the bases of Q1. The "A" side needs a base voltage of (V_O/R_O + V_Z/R_3) r_{BE} and the "B" side needs a base voltage of ($V_X/R_1+V_Y/R_2$) r_{BE}. Linearity of better than ±0.1% is readily achievable with this compensation technique.

Operational amplifier offsets are another source of error. In Figure 20, the input offset voltage and input bias current will cause an error in collector current of (V_{OS}/R_1) + I_B. A low offset op amp, such as the OP07 with less than 75 μV of V_{OS} and I_B of less than ±3 nA, is recommended. The OP22/OP32, a programmable micropower op amp, should be considered if low power consumption or single-supply operation is needed. The value of frequency-compensating capacitor (C_O) is dependent on the op amp frequency response and peak collector current. Typical values for C_O range from 30 pF to 300 pF.

FOUR-QUADRANT MULTIPLIER
A simplified schematic for a four-quadrant log/antilog multiplier is shown in Figure 21. As with the previously discussed one-quadrant multiplier, the circuit makes $I_O = I_1\, I_2/I_3$. The two input currents, I_1 and I_2, are each offset in the positive direction. This positive offset is then subtracted out at the output stage. Assuming ideal op amps, the currents are:

$$I_1 = \frac{V_X}{R_1} + \frac{V_R}{R_2},\ I_2 = \frac{V_Y}{R_1} + \frac{V_R}{R_2}$$

$$\quad (11)$$

$$I_O = \frac{V_X}{R_1} + \frac{V_Y}{R_1} + \frac{V_R}{R_2} + \frac{V_O}{R_O},\ I_3 = \frac{V_R}{R_2}$$

From $I_O = I_1\, I_2/I_3$, the output voltage will be:

$$V_O = \frac{R_O R_2}{R_1^2}\frac{V_X V_Y}{V_R} \quad (12)$$

MAT02

Collector-current range is the key design decision. The inherently low r_{BE} of the MAT02 allows the use of a relatively high collector current. For input scaling of ± 10 V full-scale and using a 10 V reference, we have a collector-current range for I_1 and I_2 of:

$$\left(\frac{-10}{R_1}+\frac{10}{R_2}\right)\le I_C \le \left(\frac{10}{R_1}+\frac{10}{R_2}\right) \tag{13}$$

Practical values for R_1 and R_2 would range from 50 kΩ to 100 kΩ. Choosing an R_1 of 82 kΩ and R_2 of 62 kΩ provides a collector-current range of approximately 39 µA to 283 µA. An R_O of 108 kΩ will then make the output scale factor 1/10 and $V_O = V_X V_Y/10$. The output, as well as both inputs, are scaled for ± 10 V full scale.

Linear error for this circuit is substantially improved by the small correction voltage applied to the base of Q1 as shown in Figure 21. Assuming an equal bulk emitter resistance for each MAT02 transistor, then the error is nulled if:

$$(I_1 + I_2 - I_3 - I_O)\, r_{BE} + \rho V_O = 0$$

The currents are known from the previous discussion, and the relationship needed is simply:

$$V_O = \frac{r_{BE}}{R_O}\, V_O \tag{14}$$

The output voltage is attenuated by a factor of r_{BE}/R_O and applied to the base of Q1 to cancel the summation of voltage drops due to $r_{BE}I_C$ terms. This will make In $(I_1\, I_2/I_3\, I_O)$ more nearly zero which will thereby make $I_O = I_1\, I_2/I_3$ a more accurate relationship. Linearity of better than 0.1% is readily achievable with this circuit if the MAT02 pairs are carefully kept at the same temperature.

MULTIFUNCTION CONVERTER

The multifunction converter circuit provides an accurate means of squaring, square rooting, and of raising ratios to arbitrary powers. The excellent log conformity of the MAT02 allows a wide range of exponents. The general transfer function is:

$$V_O = V_Y \left(\frac{V_Z}{V_X}\right)^m \tag{15}$$

V_X, V_Y, and V_Z are input voltages and the exponent "m" has a practical range of approximately 0.2 to 5. Inputs V_X and V_Y are often taken from a fixed reference voltage. With a REF01 providing a precision +10 V to both V_X and V_Y, the transfer function would simplify to:

$$V_O = 10 \left(\frac{V_Z}{10}\right)^m \tag{16}$$

As with the multiplier/divider circuits, assume that the transistor pairs have excellent matching and are at the same temperature. The In I_{SA}/I_{SB} will then be zero. In the circuit of Figure 22, the voltage drops across the base-emitter junctions of Q1 provide:

$$\frac{R_B}{R_B +\, KR_A}\, V_A = \frac{kT}{q}\, In\frac{I_Z}{I_X} \tag{17}$$

I_Z is V_Z/R_1 and I_X is V_X/R_1. Similarly, the relationship for Q2 is:

$$\frac{R_B}{R_B +\left(1-K\right)R_A}\, V_A = \frac{kT}{q}\, In\frac{I_O}{I_Y} \tag{18}$$

I_O is V_O/R_O and I_Y is V_Y/R_1. These equations for Q1 and Q2 can then be combined.

$$\frac{R_B + KR_A}{R_B +\left(1-K\right)R_A}\, In\frac{I_Z}{I_X} = In\frac{I_O}{I_Y} \tag{19}$$
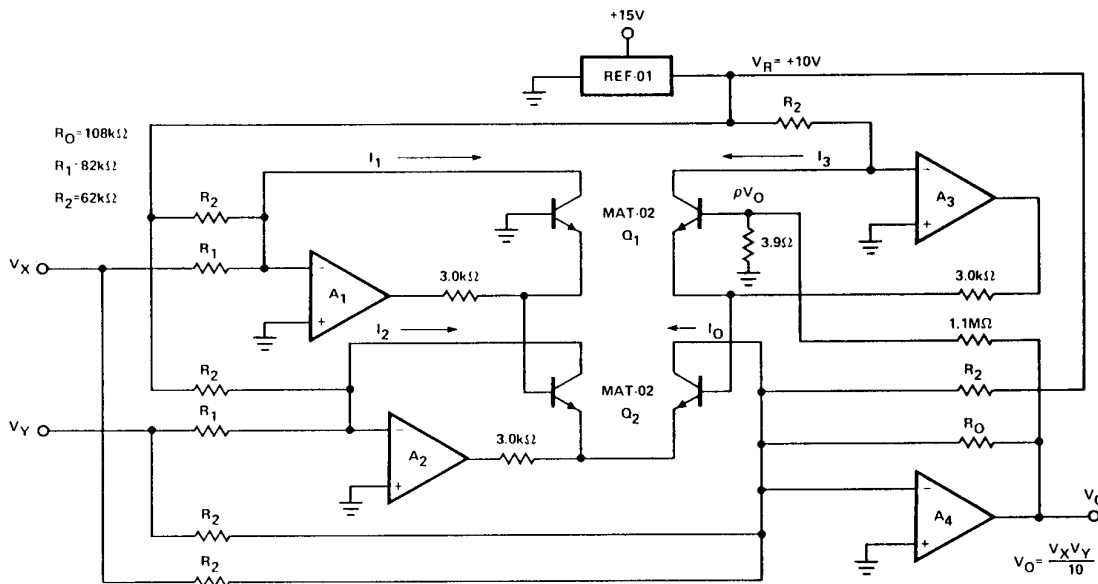

Figure 21. Four-Quadrant Multiplier

Substituting in the voltage relationships and simplifying leads to:

$$V_O = \frac{R_O}{R_1} V_Y \left(\frac{V_Z}{V_X} \right)^m, \text{ where}$$

(20)

$$m = \frac{R_B + KR_A}{R_B + (1-K)R_A}$$

The factor "K" is a potentiometer position and varies from zero to 1.0, so "m" ranges from $R_B/(R_A + R_B)$ to $(R_B + R_A)/R_B$. Practical values are 125 Ω for R_B and 500 Ω for R_A; these values will provide an adjustment range of 0.2 to 5.0. A value of 100 kΩ is recommended for the R_1 resistors assuming a full-scale input range of 10 V. As with the one-quadrant multiplier/divider circuit previously discussed, the V_X, V_Y, and V_Z inputs must all be positive.

The op amps should have the lowest possible input offsets. The OP07 is recommended for most applications, although such programmable micropower op amps as the OP22 or OP32 offer advantages in low-power or single-supply circuits. The micropower op amps also have very low input bias-current drift, an important advantage in log/antilog circuits. External offset nulling may be needed, particularly for applications requiring a wide dynamic range. Frequency compensating capacitors, on the order of 50 pF, may be required for A_2 and A_3. Amplifier A_1 is likely to need a larger capacitor, typically 0.0047 μF, to assure stability.

Accuracy is limited at the higher input levels by bulk emitter resistance, but this is much lower for the MAT02 than for other transistor pairs. Accuracy at the lower signal levels primarily depends on the op amp offsets. Accuracies of better than 1% are readily achievable with this circuit configuration and can be better than ±0.1% over a limited operating range.

FAST LOGARITHMIC AMPLIFIER
The circuit of Figure 23 is a modification of a standard logarithmic amplifier configuration. Running the MAT02 at 2.5 mA per side (full-scale) allows a fast response with wide dynamic range. The circuit has a 7 decade current range, a 5 decade voltage range, and is capable of 2.5 μs settling time to 1% with a 1 V to 10 V step.

The output follows the equation:

$$V_O = \frac{R_3 + R_2}{R_2} \frac{kT}{q} In \frac{V_{REF}}{V_{IN}}$$

(21)

The output is inverted with respect to the input, and is nominally –1 V/decade using the component values indicated.

LOW-NOISE ×1000 AMPLIFIER
The MAT02 noise voltage is exceptionally low, only 1 nV/$\sqrt{\text{Hz}}$ at 10 Hz when operated over a collector-current range of 1 mA to 4 mA. A single-ended ×1000 amplifier that takes advantage of this low MAT02 noise level is shown in Figure 24. In addition to low noise, the amplifier has very low drift and high CMRR. An OP32 programmable low-power op amp is used for the second stage to obtain good speed with minimal power consumption. Small-signal bandwidth is 1 MHz, slew rate is 2.4 V/μs, and total supply current is approximately 2.8 mA.
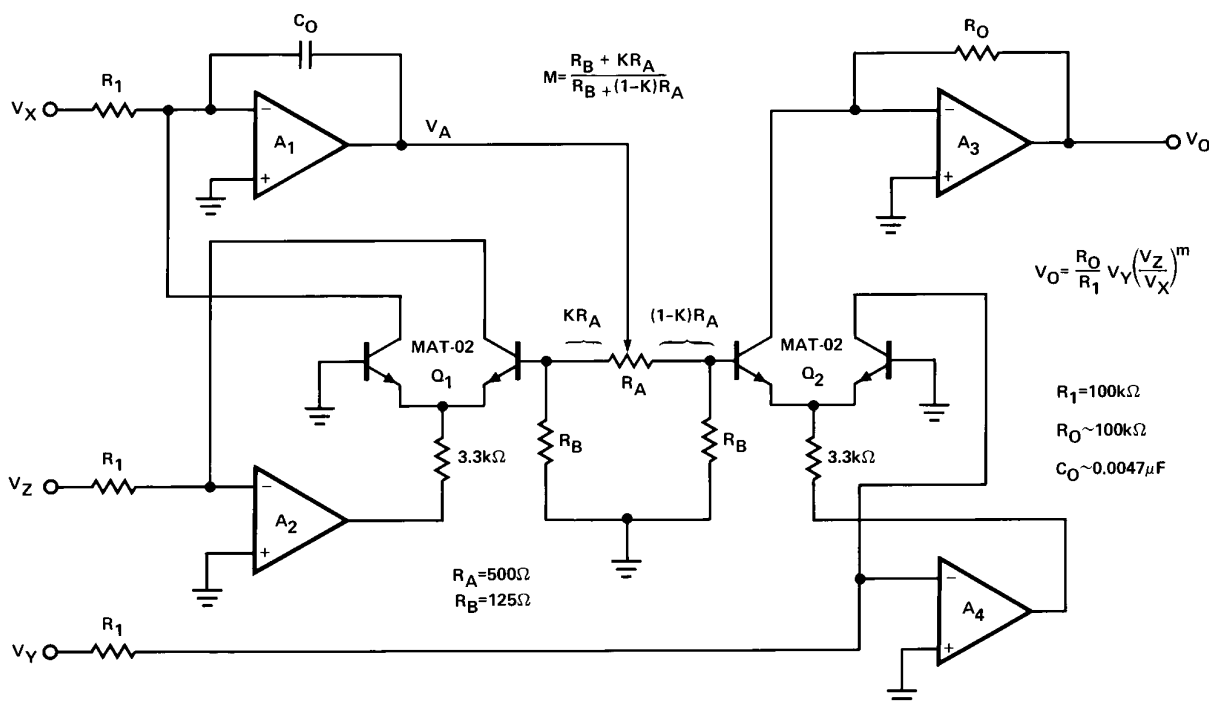

Figure 22. Multifunction Converter

MAT02

Transistors Q2 and Q3 form a 2 mA current source (0.65 V/ 330 Ω ~ 2 mA). Each collector of Q1 operates at 1 mA. The OP32 inputs are 3 V below the positive supply voltage ($R_L I_C$ ~ 3 V). The OP32's low input offset current, typically less than 1 nA, and low offset voltage of 1 mV cause negligible error when referred to the amplifier input. Input stage gain is $g_m R_L$, which is approximately 100 when operating at I_C of 1 mA with R_L of 3 kΩ. Since the OP32 has a minimum open-loop gain of 500,000, total open-loop gain for the composite amplifier is over 50 million. Even at closed-loop gain of 1000, the gain error due to finite open-loop gain will be negligible. The OP32 features excellent symmetry of slew-rate and very linear gain. Signal distortion is minimal.

Frequency compensation is very easy with this circuit; just vary the set-resistor R_S for the desired frequency response. Gain-bandwidth of the OP32 varies directly with the supply

Figure 23. Fast Logarithmic Amplifier

Figure 24. Low-Noise, Single-Ended X1000 Amplifier

current. A set resistor of 549 kΩ was found to provide the best step response for this circuit. The resultant supply current is found from:

$$R_{SET} = \frac{(V+)-(V-)-(2\,V_{BE})}{I_{SET}},\ I_{SY}=15\,I_{SET} \qquad (22)$$

The I_{SET}, using ±15 V supplies and an R_{SET} of 549 kΩ, is approximately 52 μA which will result in supply current of 784 μA.

Dynamic range of this amplifier is excellent; the OP32 has an output voltage swing of ±14 V with a ±15 V supply.

Input characteristics are outstanding. The MAT02F has offset voltage of less than 150 μV at 25°C and a maximum offset drift of 1 μV/°C. Nulling the offset will further reduce offset drift. This can be accomplished by slightly unbalancing the collector load resistors. This adjustment will reduce the drift to less than 0.1 μV/°C.

Input bias current is relatively low due to the high current gain of the MAT02. The minimum β of 400 at 1 mA for the MAT02F implies an input bias current of approximately 2.5 μA. This circuit should be used with signals having relatively low source impedance. A high source impedance will degrade offset and noise performance.

This circuit configuration provides exceptionally low input noise voltage and low drift. Noise can be reduced even further by raising the collector currents from 1 mA to 3 mA, but power consumption is then increased.
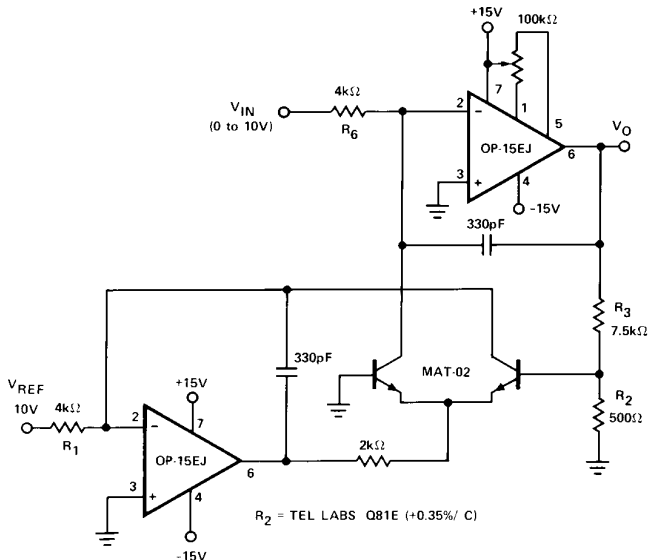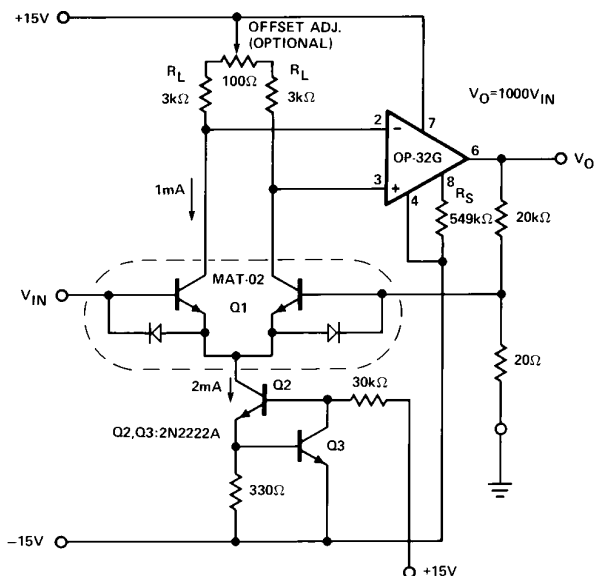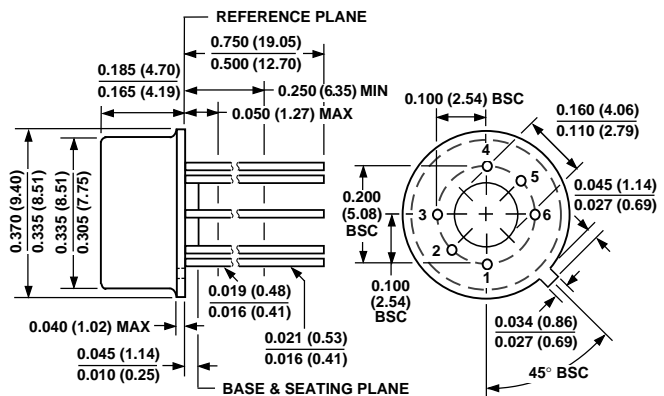
OUTLINE DIMENSION
Dimensions shown in inches and (mm).

6-Lead Metal Can
(TO-78)